The circulation of cerebral blood flow (CBF) is driven by cerebral perfusion pressure (CPP), which is defined as the vascular pressure gradient across the cerebral bed and can be calculated as the difference between arterial blood pressure (ABP) and pressure in cortical or bridging veins.\textsuperscript{15,24} Due to difficulties in measuring the pressure of bridging veins, invasive intracranial pressure (ICP) measurements are used instead as an approximation, defining CPP as ABP − ICP.\textsuperscript{1,26,34,39} Cerebral perfusion pressure in clinical practice is considered an estimations of cerebral perfusion pressure (CPP), which is clinically monitored through arterial blood pressure (ABP) and invasive measurements of intracranial pressure (ICP). Based on critical closing pressure (CrCP), the authors introduce a novel method for a noninvasive estimator of CPP (eCPP).

**METHODS**
Data from 280 head-injured patients with ABP, ICP, and transcranial Doppler ultrasonography measurements were retrospectively examined. CrCP was calculated with a noninvasive version of the cerebrovascular impedance method. The eCPP was refined with a predictive regression model of CrCP-based estimation of ICP from known ICP using data from 232 patients, and validated with data from the remaining 48 patients.

**RESULTS**
Cohort analysis showed eCPP to be correlated with measured CPP (R = 0.851, p < 0.001), with a mean ± SD difference of 4.02 ± 6.01 mm Hg, and 83.3% of the cases with an estimation error below 10 mm Hg. eCPP accurately predicted low CPP (< 70 mm Hg) with an area under the curve of 0.913 (95% CI 0.883–0.944). When each recording session of a patient was assessed individually, eCPP could predict CPP with a 95% CI of the SD for estimating CPP between multiple recording sessions of 1.89–5.01 mm Hg.

**CONCLUSIONS**
Overall, CrCP-based eCPP was strongly correlated with invasive CPP, with sensitivity and specificity for detection of low CPP that show promise for clinical use.

http://thejns.org/doi/abs/10.3171/2014.10.JNS14613

**KEY WORDS**
cerebral perfusion pressure; critical closing pressure; noninvasive model; transcranial Doppler ultrasonography; vascular disorders

**ABBREVIATIONS**
ABP = arterial blood pressure; AUC = area under the curve; CBF = cerebral blood flow; CPP = cerebral perfusion pressure; CrCP = critical closing pressure; CVR = cerebrovascular resistance; eCPP = noninvasive estimator of CPP; FV = flow velocity; GCS = Glasgow Coma Scale; GOS = Glasgow Outcome Scale; ICP = intracranial pressure; IQR = interquartile range; MCA = middle cerebral artery; nICP = noninvasive estimator of ICP; ROC = receiver operating characteristic; TAU = time constant of the cerebrovascular arterial bed; TBI = traumatic brain injury; TCD = transcranial Doppler.
sential monitored parameter for head-injury management protocols, even though ideal CPP has been poorly delineated. The invasive part of CPP calculation is ICP, the invasive nature of which can make the calculation of CPP and thus the CPP-oriented management unfeasible, such as in some clinical scenarios in which invasive measurement of ICP is either not available or unobtainable (i.e., for patients with contraindications for direct measurement). In contrast, ABP can be measured and monitored noninvasively, i.e., with a Finapres finger plethysmograph, the use of which has been shown to provide a good level of agreement between Finapres-derived indices of cerebral autoregulation and their corresponding estimates obtained from invasive measurements of aortic ABP.

Cerebral perfusion pressure has been approximated noninvasively with various methodologies in the past, based on ABP and transcranial Doppler (TCD) ultrasonography approximations of CBF. The use of these methodologies is promising as their estimation accuracy is improving. We have created a new method for assessing CPP noninvasively using a model based on the concept of critical closing pressure (CrCP), requiring ABP and TCD flow velocity (FV) measurements.

Critical closing pressure denotes a threshold of ABP, below which the local microvascular blood pressure is inadequate to prevent collapse and cessation of blood flow. As CrCP is associated with the vasomotor tone of small blood vessels, knowledge of its behavior has been recognized as able to provide valuable information regarding the state of cerebral hemodynamics in different pathologies. We have recently introduced a new method for estimating CrCP that is an apparent improvement on traditional methodology, in which the new, impedance model–based method does not render negative values. However, this method is invasive, as ICP measurements are required, possibly limiting its clinical applications in situations in which measuring ICP is not an option. For this reason, an equivalent noninvasive version of this model has been introduced, which only requires measurements of ABP and FV. The primary aim of this study was to use the CrCP method for a noninvasive assessment of CPP in a large group of head-injured patients.

Methods

Patient Population

The presented analysis was performed as part of an anonymous clinical audit, with approval of the Neurocritical Care Users Committee of Addenbrooke’s Hospital in Cambridge, the United Kingdom. This retrospective study included prospectively collected data from 280 sedated and ventilated patients with head injuries (78.2% male, median age 29 years, interquartile range [IQR] 20–43 years), hospitalized in the Neurocritical Care Unit of Addenbrooke’s Hospital between 2002 and 2011. The demographics of the patients are summarized in Table 1. All patients suffered a traumatic brain injury (TBI) and had an abnormal CT scan of the head. Patients were sedated, ventilated, and managed in the Neurocritical Care Unit with a tiered therapeutic protocol aiming for an ICP < 25 mm Hg and CPP around 60–70 mm Hg. The median preintubation Glasgow Coma Scale (GCS) score of the patients was 6 (range 3–15), while the Glasgow Outcome Scale (GOS) score, assessed 6 months after injury, varied from good outcome to death: 144 patients (51.4%) had a favorable outcome (no disability to moderate disability), while 63 patients (22.5%) died. Patients remaining in a persistent vegetative state (n = 9, or 3.2% of the total number of patients) were excluded from the study. The data included daily recordings of ABP, ICP, and TCD, performed under a standard clinical brain monitoring protocol, in a total of 780 recording periods.

Monitoring and Data Analysis

To monitor ABP, a pressure monitoring kit (Baxter Healthcare) at the radial artery was used, zeroed at the level of the heart. Monitoring of ICP was performed via an intraparenchymal probe (Codman & Shurtleff, or Camino Laboratories). Cerebral blood FV was measured from the middle cerebral artery (MCA) with a 2-MHz probe and monitored with the Doppler Box (DWL Compumedics) or Neuroguard (Medasonics, Inc.). The TCD recordings were performed on a daily basis for periods ranging from 10 minutes up to 1 hour, starting from the day of initiation of invasive monitoring. Termination of the monitoring was decided based on clinical grounds. An analog–digital converter (DT2814 or DT9801, Data Translation) was used to digitize the raw data signals at a sampling frequency of 50 Hz, which were then recorded using WREC (Warsaw University of Technology), BioSAAn (University of Cambridge), or ICM+ (Cambridge Enterprise, http://www.neurosurg.cam.ac.uk/icmplus/) software. Heart rate was calculated using spectral position of the peak associated with the first harmonic of ABP. All calculations, including mean values of ABP, ICP, FV, and CPP, were performed over a sliding window of 10 seconds.

Calculation of Noninvasive CrCP and CPP

Critical closing pressure (expressed in mm Hg) was estimated through a noninvasive version of the impedance CrCP methodology, based on ABP and TCD FV (see Appendix):

\[
CrCP = ABP - \frac{1}{\sqrt{\frac{CVR \cdot Ca \cdot HR \cdot 2\pi}{1}}} + 1
\]

[Eq. 1]

CVR denotes cerebrovascular resistance, Ca expresses arterial compliance of the cerebral bed, and HR represents heart rate (beats/sec).

To create and assess the model for the noninvasive estimator of CPP (eCPP), we dichotomized our set cohort with 232 patients (including 455 recordings) and the validation group with 48 patients (including 325 recordings).

Because the invasive part of CPP is ICP, we used the formation group to render a noninvasive estimator of ICP (nICP) based on a regression analysis of known ICP with CrCP (Eq. 1): nICP = 0.266 · CrCP + 7.026 (p < 0.001; R = 0.340, F = 59.225, N = 455). Details of the regression analysis are presented in Table 2.
Following the introduction of nICP, eCPP (in mm Hg) can then be rendered as:

\[ eCPP = ABP - nICP \]

or

\[ eCPP = ABP \cdot \left[ 0.734 - \frac{0.266}{\sqrt{(CVR \cdot Ca \cdot HR^2 + 1)}} \right] - 7.026 \]  

[Eq. 2]

In this way, eCPP is associated with physiological parameters of CVR, compliance, and heart rate, with ABP and FV as the required measurements. The performance of the new estimator was tested by comparing eCPP against invasive CPP, using data from the validation group.

The dichotomization of the total population of patients into 2 groups (formation and validation) was based on an optimization procedure for exploiting in full the available set of data. For this reason, a simple minimum requirement criterion was set, in which the validation group included only patients with a minimum of 5 or more recording sessions per patient. This selection subsequently dictated the number of patients to be included in the second group, used for formation of eCPP. Dichotomizing the cohort of patients in this way presented 2 benefits: 1) the multirecording validation portion of the study allowed for the determination of the correlation between eCPP and CPP using repetitive measurements from individual patients, and 2) the high number of recordings included in the formation group increased the statistical power of the regression model, hence rendering a more accurate eCPP. A full overview of the terminology used in this study is presented in Table 3.

### Statistical Analysis

Statistical analysis of the data was conducted with SPSS statistical software (version 20, IBM). The analysis included bivariate correlations, with R representing the Pearson correlation coefficient, and the level of significance (p value) set at 0.05. Results are presented in a mean regression model, hence rendering a more accurate eCPP.

#### TABLE 3. Terminology of used parameters

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Term</th>
<th>Units</th>
</tr>
</thead>
<tbody>
<tr>
<td>ABP</td>
<td>Arterial blood pressure</td>
<td>mm Hg</td>
</tr>
<tr>
<td>Ca</td>
<td>Cerebral arterial compliance</td>
<td>cm/mm Hg</td>
</tr>
<tr>
<td>CaBV</td>
<td>Cerebral arterial blood volume</td>
<td>cm³</td>
</tr>
<tr>
<td>CBF</td>
<td>Cerebral blood flow</td>
<td>cm/sec</td>
</tr>
<tr>
<td>CPP</td>
<td>Cerebral perfusion pressure</td>
<td>mm Hg</td>
</tr>
<tr>
<td>CrCP</td>
<td>Critical closing pressure</td>
<td>mm Hg</td>
</tr>
<tr>
<td>CrCPI</td>
<td>Invasive model of critical closing pressure</td>
<td>mm Hg</td>
</tr>
<tr>
<td>CVR</td>
<td>Noninvasive cerebrovascular resistance</td>
<td>mm Hg/(cm/sec)</td>
</tr>
<tr>
<td>CVRI</td>
<td>Invasive cerebrovascular resistance</td>
<td>mm Hg/(cm/sec)</td>
</tr>
<tr>
<td>eCPP</td>
<td>Noninvasive estimator of CPP</td>
<td>mm Hg</td>
</tr>
<tr>
<td>FV</td>
<td>Blood flow velocity</td>
<td>cm/sec</td>
</tr>
<tr>
<td>HR</td>
<td>Heart rate</td>
<td>beat/min</td>
</tr>
<tr>
<td>ICP</td>
<td>Intracranial pressure</td>
<td>mm Hg</td>
</tr>
<tr>
<td>nICP</td>
<td>Noninvasive estimator of ICP</td>
<td>mm Hg</td>
</tr>
<tr>
<td>Sa</td>
<td>Cross-sectional area of the insonated vessel</td>
<td>cm²</td>
</tr>
<tr>
<td>TAU</td>
<td>Time constant of the cerebrovascular arterial bed</td>
<td>sec</td>
</tr>
</tbody>
</table>

### TABLE 2. Summary of regression analysis parameters

<table>
<thead>
<tr>
<th>Variable</th>
<th>Coefficients</th>
<th>SEM</th>
<th>95% CI</th>
</tr>
</thead>
<tbody>
<tr>
<td>CrCP</td>
<td>0.266</td>
<td>0.035</td>
<td>0.198–0.333</td>
</tr>
<tr>
<td>Constant</td>
<td>7.026</td>
<td>1.361</td>
<td>4.352–9.700</td>
</tr>
</tbody>
</table>

* Model summary (nICP): R = 0.340, F = 59.225, p < 0.001.
Noninvasive CPP based on CrCP ± SD format. Normal distribution was established with the Shapiro-Wilk test. The Bland-Altman method was used to determine the agreement between measured parameters and their noninvasive estimations. A receiver operating characteristic (ROC) was further used to determine the ability of eCPP to predict CPP, presented with areas under the curve (AUC); the predicting ability is considered reasonable when the AUC is higher than 0.7 and strong when the AUC exceeds 0.8. The classification decision tree was created with the Chi-squared Automatic Interaction Detection (CHAID) growing method.

Results
Comparison of eCPP to Measured CPP for Patients as a Cohort

When we assessed the group of patients as a cohort, the averaged per patient eCPP was strongly correlated with the invasively measured CPP (R = 0.851, p < 0.001, n = 48; Fig. 1 left), with a mean ± SD difference between CPP and eCPP of 4.02 ± 6.01 mm Hg (Fig. 1 right). In total, 83.3% of the cases (40 patients) had an absolute estimation error of eCPP to CPP below 10 mm Hg.

The eCPP maintained its estimation accuracy when we assessed the group of 48 patients as a cohort of recordings (n = 325), with a correlation to CPP of R = 0.813, a mean difference of 3.70 ± 8.70 mm Hg, and with 259 (79.7%) of 325 recordings with an absolute estimation error less than 10 mm Hg (IQR 2.47–6.09 mm Hg).

Further analysis of the recordings with a classification decision tree indicated the absolute estimation errors for various ranges of CPP: for CPP greater than 80.19 mm Hg, the absolute estimation error of eCPP was 4.31 ± 2.86 mm Hg (97 recordings), followed by a range of CPP between 63.01 and 80.19 mm Hg, which had an absolute estimation error of 5.55 ± 4.26 mm Hg (131 recordings). The distribution of the absolute error of eCPP – CPP across the range of CPP values is demonstrated in Fig. 2.

Low CPP Prediction Analysis
An ROC curve analysis was used to determine the ability of eCPP to predict a low value of CPP in 325 recordings. Three different limits were set for CPP: 50, 60, and 70 mm Hg (Table 4). In this analysis, eCPP accurately predicted low CPP, with an AUC greater than 0.8 for all 3 limits (Table 4, Fig. 3).

Temporal Analysis of eCPP as an Estimator of Invasive CPP

In temporal analysis, each patient was assessed individually, rendering an individual correlation coefficient and a mean ± SD difference of eCPP from CPP between recording sessions. These individual results were then averaged for all patients in the application group, resulting in an eCPP that was found to be strongly correlated with CPP (mean R = 0.733, range 0.231–0.993). Examples of individual correlations between eCPP and CPP for patients are presented in Fig. 4.

For each patient, eCPP presented a mean difference from CPP of 3.45 mm Hg (range –4.69 to 19.03 mm Hg), and a mean SD of this difference of 5.52 mm Hg (range 1.52–10.76 mm Hg). These data imply a 95% CI of the SD for estimating CPP within 1 recording session of a patient to be 1.89–5.01 mm Hg.

Examples of how eCPP approximates changes of CPP in various scenarios captured during recording sessions of patients with TBI are presented in Fig. 5. Figure 6 further demonstrates in detail how the calculation of eCPP is affected by changes in its input parameters, consisting of monitored signals and estimated modules, during an event of arterial hypotension in a recording session of a single patient.

Discussion
We have constructed a new model for a noninvasive assessment of CPP based on CrCP, requiring only ABP and TCD measurements, the combination of which is attempt-
Cerebral Perfusion Pressure as a Number

Many clinical protocols for post–head-injury management are focused on guidelines requiring a range or an optimum value of CPP that needs to be achieved for an adequate perfusion of the brain.\textsuperscript{7,9,12–14,22,23,31,33,35} For this reason, we sought to determine the accuracy of estimating CPP as a number by examining the group of patients as an averaged cohort.

The results indicated that measurements obtained with eCPP were highly correlated with those for invasive CPP, with a mean ± SD difference from CPP of 4.02 ± 6.01 mm Hg. In terms of absolute error, CPP was estimated by eCPP with an error margin below 10 mm Hg in more than 80% of the analyzed cases, with eCPP demonstrated to be most accurate in the CPP range of 60 to 90 mm Hg (Fig. 2). Even though there is a lack of consensus regarding the ideal range of CPP after TBI, and the error difference of more than 10 mm Hg may or may not be clinically relevant depending on the duration of such a discrepancy,\textsuperscript{4,41} both the normal CPP range of 70–85 mm Hg\textsuperscript{41} and suggestions for maintaining a CPP of at least 70 mm Hg after head injury,\textsuperscript{35} or between 50 and 70 mm Hg,\textsuperscript{7} or at a static autoregulation range (i.e., 60–70 mm Hg)\textsuperscript{82} are within the range of the highest accuracy of eCPP. This ability of eCPP to estimate CPP most accurately at an expected or suggested level of CPP seems promising for clinical use of the method.

The outcome of a patient following TBI has been known to be significantly affected by exposures to secondary insults such as systemic hypotension or intracranial hypertension, which can result in severely reduced
Noninvasive CPP based on CrCP

CPP and cerebral ischemia when CPP decreases below 50–60 mm Hg. The eCPP demonstrated a strong ability to predict low values of CPP, as examined in 3 different thresholds for CPP values below 50, 60, and 70 mm Hg. Therefore, this signifies that eCPP could act as a noninvasive indicator of potentially inadequate CPP, acting as a warning for hypoperfusion during monitoring of a patient.

Cerebral Perfusion Pressure as a Time-Varying Variable

Apart from assessing CPP solely as a number, some studies suggest that CPP is better considered as a condition of CBF, reflecting the hemodynamic status of a patient after TBI. This suggestion is based on the fact that in clinical practice, brain perfusion assessed through CPP can be underestimated due to ABP monitoring devices.

![ROC curve analyses for predicting low CPP with eCPP for 2 different thresholds of CPP: 50 mm Hg (left) and 70 mm Hg (right). In both cases, eCPP demonstrated a strong predictive power, indicated by the AUC values.](image1)

![Examples of individual correlations between CPP and eCPP. Each graph represents 1 patient and each open circle represents 1 recording session. The upper row (A–C) demonstrates cases of good correlations between CPP and eCPP, whereas the lower row (D–F) presents the weaker cases. Weaker cases are associated with overestimation of CPP.](image2)
measuring readings from peripheral vessels and calibrated at the heart level and not at the head level. Therefore, brain perfusion is better represented by global CBF as assessed through MRI or PET, instead of a numerical value of CPP. However, these existing methods for accurately assessing CBF are not suitable for continuous monitoring, the role of which is thereby served by CPP. A CPP that is considered not only as a value but rather as a time variable can then indicate changes in CBF over time, therefore being able to characterize changing hemodynamic needs, such as in cases of arterial hypotension or intracranial hypertension insults that would threaten to reduce CBF.

In this part of our study, each patient was assessed individually, with the accuracy levels of eCPP improving in comparison with the respective cohort analysis (mean ± SD differences from CPP of 3.45 ± 5.52 mm Hg vs 4.02 ± 6.01 mm Hg, respectively). This finding implies that eCPP provides a more accurate CPP estimation when CPP is assessed over time, i.e., for following changes in CPP during a monitoring session when ABP and TCD measurements are performed. The underlying factors for this difference might have to do with how ABP- and TCD-derived information is being exploited; in cohort analysis the information regarding ABP and FV dynamics, as contained in CrCP, is averaged out, thereby potentially “hiding” phenomena that could influence CPP for a short period of time. In contrast, in time analysis these phenomena, such as a drop in ABP, are captured, therefore improving the accuracy of eCPP. This was further demonstrated in the examples shown in Fig. 5, in which eCPP correctly depicted a variety of changes and fluctuations of CPP.

The Role of ICP

Intracranial pressure has an important role in TBI management, as phenomena of intracranial hypertension can lead to a decrement in CPP and a potential decrease in CBF, causing secondary ischemic insults. In fact, many of the studies recommending CPP thresholds are confounded by high ICP, therefore further signifying its clinical role. However, focusing solely on ICP would not be sufficient, as from a physiological viewpoint, both individual components of CPP (ICP and ABP) have been shown to affect CBF and consist of independent predictors of outcome after TBI. Hence, monitoring and management of CPP will remain one of the cornerstones of TBI management, even though it is recognized that further work is required in terms of patient-specific thresholds. For this reason, the development of noninvasive methods to monitor CPP is reasonable and could provide an additional option in resource-limited settings or for patients who have contraindications for invasive monitoring.

The invasive character of ICP has also been the limiting factor for these noninvasive CPP assessments, with high ICP resulting in overestimation of CPP. Therefore, information derived from both ABP and TCD measurements is being used, attempting to compensate for the absence of invasive ICP measurements. In contrast to other methodologies, the basis of the eCPP method consists of a regression analysis, constructed with a large number of TBI recordings (455 in total), which included cases in which ICP is either low (5 mm Hg) or very high (above 40 mm Hg). In this matter, eCPP contains some TCD- and ABP-derived descriptive information about these cases, encapsulated in the form of cerebrovascular compliance and resistance in CrCP. This aided eCPP in capturing circumstances of low and very low CPP, demonstrated with high levels of sensitivity and specificity for detecting reduced CPP. Even though high ICP does cause a CPP overestimation by eCPP, restricting its capability in terms of estimating CPP as an absolute number, the loss of precision at high ICP is mitigated by its ability to detect low CPP.

Benefits of Using CrCP for CPP Estimation

A benefit of using impedance CrCP for estimating CPP
Noninvasive CPP based on CrCP

is that it allowed us to associate the CPP estimator with further physiological parameters such as heart rate and measures of the resistance and compliance of the cerebrovascular bed. eCPP subsequently contains the product of CVR and compliance, relating eCPP to the physiological measurement of TAU, which is an estimate of how fast the cerebral arterial bed is filled by blood volume after a sudden change in ABP during 1 cardiac cycle. Due to this relationship, eCPP as a function of TAU and heart rate can then take into account changes in primary variables describing cerebral hemodynamics and cardiac function, enhancing its physiological presence for estimating CPP.

A further advantage of having TAU in the eCPP formula is the inherited independence of eCPP from the unknown cross-sectional area of the insonated vessel, as it gets eliminated through TAU calculation (see Appendix).19

Limitations of the Study

The calculations regarding CrCP and consequently eCPP depended on information derived from ABP and FV. Measurement and monitoring of these 2 parameters pose some limitations in regard to the accuracy of the estimations. First, a good quality of recording is required, and in regard to the TCD technique, the quality depends, among other parameters, on the experience of the user for accurately insonating the targeted artery (the MCA). Moreover, unlike ABP measurements, TCD monitoring was not continuous but instead it included short recording periods for every patient on a daily basis, therefore posing a restriction on continuous eCPP assessment. The reasons behind short recordings were: 1) the needs of a neuro-intensive care environment, in which treatment of head-injured patients includes change in position or transfer (for CT/MRI scan purposes) resulting in an unavoidable interruption of TCD recordings; and 2) the limitations of the current TCD technology, regarding the limited capability of probe holders, which are not well suited for prolonged continuous recording. An expected improvement in TCD technology for continuous FV monitoring would allow full exploitation of the eCPP methodology in the future (http://www.prnewswire.com/news-releases/physionics-announces-fda-clearance-for-presto-1000-flow-monitor-for-ultrasound-cranial-monitoring-184153001.html).

The use of radial artery ABP zeroed at the level of the heart instead of actual blood pressure in the brain could be considered a limitation of the study, in terms of how well the level of peripheral ABP can approximate the respective intracranial ABP. Heart-level calibration leads to an overestimation of actual CPP at the head level,17 with this difference also affecting the impedance calculation that derives information from ABP measurements. However, this limitation may not have been too significant in this study because the primary comparisons between the invasive (CPP) and noninvasive calculations had a common basis, the same ABP point of measurement. Therefore, this limi-

FIG. 6. Example of how monitored signals and estimated parameters affect the calculation of eCPP during an event of arterial hypotension (gray area) in a recording session of a single patient. Monitored signals included ABP, TCD blood FV, and ICP, while estimated parameters included CPP, CVR, compliance (Ca), and time constant (TAU). A decrease in ABP with an increase in heart rate (HR) is followed by compensatory vasodilatation, reducing CVR and increasing compliance, which in turn leads to an increase in TAU and a reduction in CrCP due to decreased vasomotor tone of the small cerebral vessels. Overall, changes in the variables of the eCPP formula (see Appendix) ABP, HR, CVR, and compliance (or TAU being the product of the latter 2 variables) led to eCPP presenting an estimated decrease in CPP.
tation may not have affected the actual aims of this study; as long as the same level of ABP measurement is used, a similar estimation accuracy of CPP can be expected.

The comparison of eCPP with CPP could also be applied to a comparison between invasive ICP and nICP, as mathematically the two models (nICP and eCPP) differ only in terms of the addition of ABP in eCPP. However, even though the accuracy levels for CPP estimation are promising, a similar accuracy for ICP may not be adequate, due to the difference in magnitude between CPP and ICP. An estimation error of 5–10 mm Hg could be clinically acceptable for CPP, ranging, for example, from 60 to 90 mm Hg, but would not be sufficient for an ICP ranging from 5 to 25 mm Hg. Even though this would limit the use of CrCP for noninvasive ICP estimation, it allowed the formation of the eCPP model, which rendered encouraging results for its use in clinical practice.

The number of patients in whom the eCPP methodology was applied might pose a limitation in this study, regarding the coverage of different clinical scenarios with a small sample consisting of 48 patients. However, these patients had a high number of repetitive measurements (≥5 per patient), therefore fulfilling the purpose of the cohort’s dichotomization regarding the validation of eCPP as an accurate estimator of CPP, examined as a time-varying variable. An overall synopsis of the advantages and limitations of using eCPP is presented in Table 5.

Conclusions

The use of CrCP formed the basis of a new methodology that demonstrated promising results in regards to a noninvasive estimation of CPP. Analysis of patients as a cohort and through individual recording sessions resulted in a strong correlation between eCPP and CPP, presenting a relatively small estimation error. Most importantly, low values of CPP were well detected by eCPP, which showed strong predictive power and the ability to act as a noninvasive indicator of low or inadequate perfusion.

### Appendix

#### Calculation of Noninvasive Critical Closing Pressure (CrCP)

The basis for the noninvasive model is given by the invasive multiparameter impedance method:\textsuperscript{39}

\[
\begin{align*}
\text{CrCPi} &= \frac{ABP - CPP}{\sqrt{(\text{CVRi} \cdot \text{Ca} \cdot HR \cdot 2\pi)^2 + 1}} [\text{mm Hg}] & \text{[Eq. A]}
\end{align*}
\]

In this model, the invasive parts of the formula (containing the ICP parameter) are CPP and invasive cerebrovascular resistance (CVRi), which can be approximated as:\textsuperscript{20}

\[
\text{CVRi} = \frac{\text{CPP}}{\text{FV/Sa}} \left\frac{[\text{mm Hg}]}{[\text{cm}^3]}\right
\]

In this equation, the parameter Sa in the denominator represents the unknown cross-sectional area of the insonated vessel. Ca denoting the compliance of the cerebrovascular bed can be estimated as:\textsuperscript{20}

\[
\text{Ca} = \frac{\text{CaBV} \cdot \text{Sa}}{A_1} \left\frac{[\text{cm}^3]}{[\text{mm Hg}]}ight
\]

In this equation, $A_1$ is the fundamental harmonic amplitude of ABP, whereas CaBV is the amplitude of the fundamental harmonic of cerebral arterial blood volume (CaBV), derived by using a 10-second discrete Fourier transformation of CaBV’s time series. Changes of pulsatile CaBV in turn can be approximated by integrating the FV pulse waveform with the beat-to-beat mean removed, in the form of samples of instant and average values of FV, respectively:\textsuperscript{20}

\[
\Delta \text{CaBV}(n) = \text{Sa} \cdot \sum \text{FV(i)} - \text{meanFV)At}
\]

In this equation, $n$ is the number of the samples and $\Delta t$ is the time interval between 2 consecutive samples. Instant (sampled) arterial blood flow velocity is represented by FV(i), while mean FV represents the corresponding average value.

By having the product of Ca and CVRi in Eq. A, the parameter Sa is cancelled out, as has been described in the impedance methodology.\textsuperscript{39}

#### Calculation of Noninvasive Critical Closing Pressure

<table>
<thead>
<tr>
<th>Advantages</th>
<th>Disadvantages</th>
</tr>
</thead>
<tbody>
<tr>
<td>The estimation error of eCPP is relatively small, hence being able to provide an indication of CPP levels where invasive measurements are not available</td>
<td>Requires TCD measurements that are hard to obtain continuously for long-term monitoring of eCPP</td>
</tr>
<tr>
<td>eCPP is strongly correlated with invasive CPP, presenting a good indication of changes in CPP over time</td>
<td>Requires suitable software for a next-to-bed instant calculation, based on the monitored signals of ABP and FV</td>
</tr>
<tr>
<td>Low values of CPP are well detected by eCPP, highlighting its ability to act as a noninvasive indicator of low or inadequate perfusion</td>
<td>High ICP causes a CPP overestimation by eCPP, restricting its capability in terms of estimating CPP as an absolute number. However, the loss of precision at high ICP is mitigated by eCPP’s ability to detect low and very low CPP</td>
</tr>
<tr>
<td>Even though there is a lack of consensus regarding an ideal range of CPP after TBI, all the guideline levels are within the range of highest accuracy of eCPP</td>
<td>[\Delta \text{CaBV}(n) = \text{Sa} \cdot \sum \text{FV(i)} - \text{meanFV)At}]</td>
</tr>
<tr>
<td>eCPP has a physiological substance, as its estimation is based on physiological parameters of heart rate, cerebrovascular resistance, compliance, and cerebral time constant</td>
<td>[\text{Ca} = \frac{\text{CaBV} \cdot \text{Sa}}{A_1} \left\frac{[\text{cm}^3]}{[\text{mm Hg}]}</td>
</tr>
</tbody>
</table><p>ight] |
| eCPP is not affected by a common limitation of measuring blood flow through TCD ultrasonography as its calculation is independent of the unknown cross-sectional area of the insonated vessel, i.e., the MCA during measurement periods | [\text{CrCPi} = \frac{ABP - CPP}{\sqrt{(\text{CVRi} \cdot \text{Ca} \cdot HR \cdot 2\pi)^2 + 1}} [\text{mm Hg}] ] |</p>

\[\text{Table 5. Advantages and disadvantages of using eCPP}\]
In order to create the noninvasive version of CrCPI, we approximate CPP with ABP and thus CVRI can be now approximated noninvasively as

\[
CVR = \frac{\text{ABP}}{\text{PV} \cdot \text{Ca}} \frac{[\text{mm Hg}]}{[\text{cm}^3]}
\]

Based on these remarks, the noninvasive model of impedance CrCP (in mm Hg) is given as:

\[
CrCP = ABP \cdot \left[ 1 - \frac{1}{(CVR \cdot Ca \cdot HR \cdot 2\pi)^2} + 1 \right] \quad \text{[Eq. B]}
\]

**Association of eCPP With TAU**

The product of cerebrovascular resistance (CVR) and compliance (Ca) represents the noninvasive time constant, or TAU. Therefore, the formula for eCPP (in mm Hg) is given as:

\[
eCPP = ABP \cdot \left[ 0.734 - \frac{0.266}{(TAU \cdot HR \cdot 2\pi)^2} \right] - 7.026 \quad \text{[Eq. C]}
\]

**References**


Author Contributions
Conception and design: GV Varsos, Czosnyka. Acquisition of data: Czosnyka. Analysis and interpretation of data: GV Varsos, Brady, Hutchinson, Pickard, Czosnyka. Critically revising the article: Kolias, Smielewski, Brady, VG Varsos, Hutchinson, Pickard, Czosnyka. Reviewed submitted version of manuscript: Czosnyka. Approved the final version of the manuscript on behalf of all authors: GV Varsos. Statistical analysis: GV Varsos. Administrative/technical/material support: Czosnyka. Study supervision: Czosnyka.

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